

# Percentage of a Number: Using Decimals

You have learned that to find 1% of a number means finding  $1/100$  of it. Similarly, finding 60% of a number means finding  $60/100$  (or  $6/10$ ) of it.

In these types of expressions, the word “of” translates into **multiplication**:

$$\begin{array}{ccc} 1\% \text{ of } 90 & & 60\% \text{ of } \$700 \\ \downarrow & \text{OR} & \downarrow \\ 1\% \times 90 & & 60\% \times \$700 \end{array}$$

Next, let’s write those percentages as *decimals*. We get:

$$\begin{array}{ccc} 1\% \text{ of } 90 & & 60\% \text{ of } \$700 \\ \downarrow & \text{OR} & \downarrow \\ 0.01 \times 90 & & 0.6 \times \$700 \end{array}$$

This gives us another way to calculate a certain percentage of a number (or a percentage of some quantity):

To calculate a percentage of a number, you need to do TWO simple changes:

1. Change the percentage into a decimal.
2. Change the word “of” into multiplication.

**Example 1.** Find 70% of 80.

Following the shortcut, we write this as  $0.7 \times 80$ .

(Remember, in decimal multiplication, you multiply as if there were no decimal points, and the answer will have as many decimal digits as the total number of decimal digits in all of the factors.)

So, when you multiply  $0.7 \times 80$ , think of multiplying  $7 \times 80 = 560$ . Since 0.7 has one decimal digit, and 80 has none, the answer has one decimal digit. Thus,  $0.7 \times 80 = 56.0$  or just 56.

You can also use common sense and estimation:  $0.7 \times 80$  must be less than 80, yet more than  $1/2$  of 80, which is 40. Since  $7 \times 8 = 56$ , you know that the answer must be 56—not 5.6 or 560.

**Example 2.** Find 3% of \$4,000.

First, write this as  $0.03 \times \$4,000$ . Next, multiply without decimal points:  $3 \times \$4,000 = \$12,000$ .

Lastly, put the decimal point so that the answer will have two decimal digits: \$120.00.

**Example 3.** Find 23% of 5,500 km.

Write this as  $0.23 \times 5,500$  km and use a calculator. The answer is 1,265 km. This makes sense, because 10% of 5,500 km is 550 km, and 20% of it is 1,100 km. Therefore, 1,265 km as 23% of 5,500 km is reasonable.

1. “Translate” the expressions into multiplications by a decimal. Solve, using mental math.

a. 20% of 70 _____ × _____ = _____	b. 90% of 50 _____ × _____ = _____	c. 80% of 400 _____ × _____ = _____
d. 60% of \$8 _____ × _____ = _____	e. 9% of 3,000 _____ × _____ = _____	f. 7% of 40 L _____ × _____ = _____
g. 150% of 44 kg _____ × _____ = _____	h. 200% of 56 students _____ × _____ = _____	i. 2% of 1,500 km _____ × _____ = _____