## Math Mammoth Fractions 2

## Contents

Introduction	4
Simplifying Fractions 1	6
Simplifying Fractions 2	10
Multiply Fractions By Whole Numbers	13
Multiplying Fractions by Fractions 1	17
Multiplying Fractions by Fractions 2	20
Fraction Multiplication and Area	22
Simplifying Before Multiplying	28
Multiply Mixed Numbers	33
Multiplication as Scaling/Resizing	36
Fractions Are Divisions	40
Dividing Fractions: The Shortcut	44
Dividing Fractions: Sharing Divisions	<b>48</b>
Dividing Fractions: Fitting the Divisor	52
Dividing Fractions Summary	54
Review	56
Answers	60
Fractions Cutouts	80
More from Math Mammoth	86

## Introduction

*Math Mammoth Fractions 2* continues the study of fraction topics after *Math Mammoth Fractions 1*. I sincerely recommend that the student study the *Fractions 1* book prior to studying this book, if he has not already done so.

I have made a set of videos to match many of the lessons in this book. You can access them at https://www.mathmammoth.com/videos/fractions\_2.php

This book is meant for fifth grade, and deals in-depth with the following topics:

- simplifying fractions; including simplifying before multiplying;
- multiplication of fractions (and of mixed numbers);
- division of fractions.

We start out by simplifying fractions. Since this is the opposite of making equivalent fractions, studied in *Math Mammoth Fractions 1*, it should be easy for students to understand. We also use the same visual model, just backwards: This time the pie pieces are joined together instead of split apart.

Next comes multiplying a fraction by a whole number. Since this can be solved by repeated addition, it is not a difficult concept.

Multiplying a fraction by a fraction is first explained as taking a certain part of a fraction, in order to teach the concept. After that, students are shown the usual shortcut for the multiplication of fractions.

Then, we find the area of a rectangle with fractional side lengths, and show that the area can be found by multiplying the side lengths. Students multiply fractional side lengths to find areas of rectangles, and represent fraction products as rectangular areas.

Simplifying before multiplying is a process that is not absolutely necessary for fifth graders. I have included it here because it prepares students for the same process in future algebra studies and because it makes fraction multiplication easier.

Students also multiply mixed numbers, and study how multiplication can be seen as resizing or scaling. This means, for example, that the multiplication  $(2/3) \times 18$  km can be thought of as finding two-thirds of 18 km.

Next, we study the division of fractions. The first lesson on the topic shows how fractions can be seen *as* divisions; in other words, for example, 5/3 is the same as  $5 \div 3$ . This of course gives us a means of dividing whole numbers and getting fractional answers (for example,  $20 \div 6 = 32/6$ ).

The next lesson on the topic explores the thought of solving division problems by *multiplying*, and then introduces reciprocal numbers and the common shortcut for fraction division.

The following two lessons focus on two ways to think about division: equal sharing, and fitting the divisor (measurement division), and how they apply to fraction division. Here is an example of equal sharing: If two people equally share 4/5 of a pizza, how much will each person get? This is represented by the division  $(4/5) \div 2 = 2/5$ .

I wish you success in teaching math!

Maria Miller, the author